



1		$\left(\frac{3}{4}\right)^2, \frac{3}{5}, 0.65, \frac{3}{4}$	B1	c.a.o.	
					[1]
2		$\left(\frac{y^6}{x^8}\right)^{\frac{3}{2}}$	M1	Flip fraction or M0	
		$= \frac{y^9}{x^{12}}$	A1	or B1 for numerator and denominator	
					[2]
3	(a)	$k = 3$	B1		
	(b)	$x = \frac{2}{3}$	B1		
					[2]
4		Angle $CBD = 180^\circ - 129^\circ = 51^\circ$ (Adjacent angles on a straight line) Angle $CBD = 180 - 51^\circ - 38^\circ = 91^\circ$ (Angles sum of triangle)	M1		
		Since angle $CBD = 91^\circ \neq 90^\circ$, using the right-angle in semicircle property, BC is not a diameter of the circle.	A1 AG		
					[2]
5		$(3n-1)^2 + 2$ $= 9n^2 - 6n + 1 + 2$	M1	Expand	
		$= 9n^2 - 6n + 3$ $= 3(3n^2 - 2n + 1)$ Since 3 is a factor of the expression, then it is a multiple of 3 for all integer values of n .	A1 AG		
					[2]
6	(a)	The greatest number of marriages per 1000 males in 2014 and 2004 both occurred in the age group of 30-34 years. OR There are more marriages per 1000 males at a later age in 2014 than 2004.	B1	Accept any reasonable comparison between both graphs	
	(b)	No because <u>the mode age group for marriages per 1000 for both genders are within 30–34 years.</u>	B1	Accept any other comparison o.e.	
					[2]



7	(a)	$B' \cup A$	B1		
	(b)	$(B' \cap A) \cup (A' \cap B)$	B1		
					[2]
8		Total monthly payments = $\$113 \times 12 = \1356	M1		
		Deposit = $\$1651 - \$1356 = \$295$	M1		
		Percentage = $\frac{\$295}{\$1475} \times 100\% = 20\%$	A1		
					[3]
9	(a)	Angle $ABC = 64^\circ$	B1		
	(b)	Angle $AOC = 128^\circ$	B1		
	(c)	Angle $OAD = 64^\circ$	B1	FT from (a)	
					[3]
10		Time taken = $\frac{5408}{721} = 7.500693481 = 7.50$ hours	M1		
		Estimated time of arrival (Australian Time) is 1655			
		Singapore is Ahead by 1.50 hours	A2		
					[3]
11		$\frac{V}{184} = \left(\frac{1}{20}\right)^3$	M1	Form equation	
		$V = \left(\frac{1}{20}\right)^3 \times 184 = 0.023 \text{ m}^3$	A1		
		$2.3 \times 10^{-2} \text{ m}^3$	A1		
					[3]



12	(a)	14 hours	B1		
	(b)	$F = \frac{k}{d^2}$, where k is a constant. Let $F_1 = \frac{k}{d_1^2}$ and $d_2 = 1.2d_1$.			
		$F_2 = \frac{k}{d_2^2} = \frac{k}{(1.2d_1)^2} = \frac{25}{36} \left(\frac{k}{d_1^2} \right) = \frac{25}{36} F_1$	M1	Finds a relation between F_1 and F_2	
		Percentage = $\frac{F_1 - \frac{25}{36} F_1}{F_1} \times 100\% = 30 \frac{5}{9} \% = 30.6\% \text{ (3 s.f.)}$	A1	Accept 3 s.f.	
					[3]
13	(a)	$2pq(4p - 3q^2)$	B2	B1 for '2' B1 for pq	
	(b)	$2xy(3x - 1) + (3x - 1)$ $= (2xy + 1)(3x - 1)$	M1		
			A1		
					[4]
14		Interior angle of $C = \frac{(6-2) \times 180^\circ}{6} = 120^\circ$	M1		
		Interior angle of $B = 360^\circ - 120^\circ - 90^\circ = 150^\circ$	M1		
		Exterior angle of $B = 180^\circ - 150^\circ = 30^\circ$	M1		
		Number of sides in $B = \frac{360^\circ}{30^\circ} = 12$	A1		
		<u>Alternatively (using sum of interior angles):</u>			
		$(n-2) \times 180 = 150n$	M1	Form equation	
		$180n - 360 = 150n$ $30n = 360$ $n = 12$	A1		
					[4]



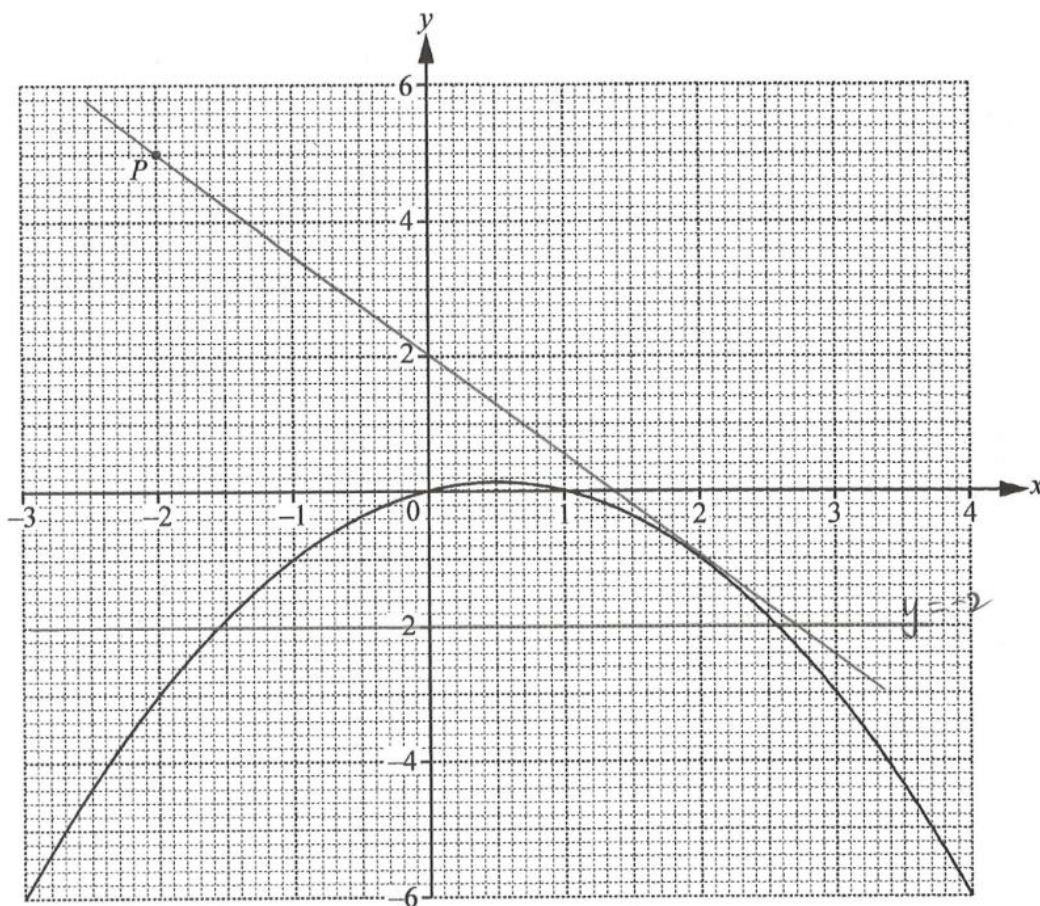
15	Let x denote the number of males in the group. Number of females = $x + 4$			
	$\frac{\text{Total height of females}}{x + 4} = 162$ $\Rightarrow \text{Total height of females} = 162x + 648$ $\frac{\text{Total height of males}}{x} = 183$ $\Rightarrow \text{Total height of males} = 183x$ $\frac{\text{Total height of students}}{2x + 4} = 171$ $\Rightarrow \text{Total height of females} = 342x + 684$	M2	M1 for any correct expression seen M1 for all correct	
	$162x + 648 + 183x = 342x + 684$ $3x = 36$ $x = 12$	M1	Find x	
	Total number of students in the group = $2(12) + 4 = 28$	A1		
				[4]
16	Perimeter of minor sector = $2r + r\theta$ Perimeter of major sector = $2r + r(2\pi - \theta)$	M1	Either seen	
	$2r + r(2\pi - \theta) = 2(2r + r\theta)$	M1	Form equation	
	$2r + 2\pi r - r\theta = 4r + 4r\theta$ $3r\theta = 2\pi r - 2r$	M1		
	$\theta = \frac{2\pi - 2}{3} = 1.427728436 = 1.428 \text{ rad (3 d.p.)}$	A1		
				[4]
17	$x^2y - ay = x^2 + 3$	M1	Remove fraction	
	$x^2y - x^2 = 3 + ay$	M1	Rearranging	
	$x^2(y - 1) = 3 + ay$ $x^2 = \frac{3 + ay}{y - 1}$	M1		
	$x = \pm \sqrt{\frac{3 + ay}{y - 1}}$	A1		
				[4]



18	(a)	$\sqrt{a^2 + 9a^2} = \frac{5\sqrt{10}}{2}$ $10a^2 = \frac{125}{2}$	M1	Form equation	
		$a^2 = \frac{25}{4}$ $a = \pm\sqrt{\frac{25}{4}} = \pm\frac{5}{2}$	A1	o.e.	
	(b)	$\overrightarrow{AB} = \begin{pmatrix} 48 \\ 37 \end{pmatrix}$	B1		
	(c)	$\overrightarrow{AC} = \begin{pmatrix} 11 \\ 13 \end{pmatrix} - \begin{pmatrix} -5 \\ 1 \end{pmatrix} = \begin{pmatrix} 16 \\ 12 \end{pmatrix} \neq k \begin{pmatrix} 48 \\ 37 \end{pmatrix}$	M1	Find $\overrightarrow{AC}$	
		Since $\overrightarrow{AC} \neq k\overrightarrow{AB}$, the AC is not a scalar multiple of AB and hence C does not lie on AB.	A1		
					[5]
19	(a)	128 grams	B1		
	(b)	$x = 7$	B1		
	(c)	1. On average, the masses of the Apples are heavier than the Bananas as the median of 128 g is larger than the median of 125 g of the Bananas. 2. The masses of the Bananas are more consistent than the Apples as the range of 44 g is lower than the range of 58 g of the Apples.	B1 B1	Must quote values Must quote values	
					[4]
20	(a)	$126 = 2 \times 3^2 \times 7$	B1		
	(b)	$k = 14$	B1		
	(c)	$x = 3 \times 7 \times 11$ $x = 231$	M1 A1	Any two factors	
					[4]



21		When $x = -2$, $y = 11$. $11 = a(-2)^2 + b(-2) + 3$ $4a - 2b = 8$ ---- (1) When $x = 4$, $y = -1$. $-1 = a(4)^2 + b(4) + 3$ $16a + 4b = -4$ ---- (2)	M1	Substitution and either equation seen	
		$(1) \times 2$ $8a - 4b = 16$ ---- (3) $(2) + (3)$ $24a = 12$	M1	Elimination or substitution s.o.i.	
		$a = \frac{1}{2}$	A1	o.e.	
		$b = -3$	A1		
					[4]
22		Angle $CBE = \text{Angle } BEC = 35^\circ$ Angle $BCE = 180^\circ - 2(35^\circ) = 110^\circ$	M1	110° s.o.i.	
		$\text{Area} = \frac{1}{2}(8)(10)\sin 110^\circ - \frac{1}{2}(8)^2 \sin 110^\circ$	M3	M1 for $ABCD$ M1 for BCE M1 for difference	
		$= 45.1052458 = 45.1 \text{ cm}^2$ (3 s.f.)	A1		
					[5]
23	(a)	$x = 0.5$	B1	o.e.	
	(b)	$x - x^2 = -4$ $\Rightarrow \frac{1}{2}(x - x^2) = -2$ $\Rightarrow y = -2$	M1	Find equation of line (no need to draw on grid, can be implied in working seen)	
		$x = -1.55$ or $x = 2.55$	A1		
	(ci)	Drawing of tangent (Refer to graph on page 7)	B1		
	(cii)	Gradient $= \frac{5-2}{-2-0} = -\frac{3}{2}$	M1	s.o.i.	
		$y = -\frac{3}{2}x + 2$	A1	o.e.	
					[6]



24	(a)	Using sine rule, $\frac{\sin \angle DMS}{4140} = \frac{\sin 29^\circ}{2392}$ $\sin \angle DMS = \frac{4140 \sin 29^\circ}{2392}$	M1	o.e.	
		Angle $DMS = 57.04452664^\circ = 57.0^\circ$ (1 d.p.)	A1	c.a.o.	
	(b)	Bearing $= 360^\circ - (180^\circ - (180^\circ - 70^\circ + 29^\circ))$ $= 319^\circ$	M1 A1	$180^\circ - 70^\circ$ s.o.i.	
					[4]

END OF MARKING SCHEME



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Mathematics 4048/01
Syllabus 4048 Paper 1
SUGGESTED Solutions & Marking Scheme Mark Allocation
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