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4049/02

14 September 2021

2 hours 15 minutes

Candidates answer on the Question Paper.

No Additional Materials are required.

READ THESE INSTRUCTIONS FIRST

Write your centre number, index number and name in the spaces at the top of this page.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE ON ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an approved scientific calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 90.

For Examiner's Use
90

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial expansion

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{r!(n-r)!} = \frac{n(n-1) \dots (n-r+1)}{r!}$

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$

$$\sec^2 A = 1 + \tan^2 A$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A$$

$$\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$\sin 2A = 2 \sin A \cos A$$

$$\cos 2A = \cos^2 A - \sin^2 A = 2 \cos^2 A - 1 = 1 - 2 \sin^2 A$$

$$\tan 2A = \frac{2 \tan A}{1 - \tan^2 A}$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2} ab \sin C$$

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Answer **all** the questions.

- 1 (a) Express $\frac{16x-14x^2-1}{(3x-1)(2x+1)^2}$ in partial fractions. [5]

- (b) A right pyramid has a square base of side $(\sqrt{6} + \sqrt{3})$ m and a height of h m.

The volume of the pyramid is $(6 + \sqrt{8}) \text{ m}^3$. Without using a calculator, show that h can be expressed as $a + b\sqrt{2}$, where a and b are integers.

[3]

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- 2 (a) Given that $p > \frac{1}{3}$, explain why the equation $3^{2x+1} = 6(3)^{x-1} - p$ has no real solutions.

[4]

- (b) Find the **exact** range of values of the constant a for which the line $y = 2x - \frac{a^2}{2}$ intersects the curve $y = x^2 - ax - 4$ at two distinct points. [5]

- 3 The equation of a curve is $y = \cos^3\left(\frac{x}{2} + \frac{\pi}{4}\right)$.

Find the value(s) of x for $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$ where the equation of the normal to the curve is $x = k$, where k is a constant.

[4]

- 4 A glass of hot liquid is placed on a table to cool. The following table shows the measured values of the temperature of the liquid, $T^{\circ}\text{C}$ after n minutes.

n (minutes)	10	20	30	50
T ($^{\circ}\text{C}$)	76.5	57.4	45.9	34.6

- (i) On the grid on page 9, plot $\ln(T - 28)$ against n and draw a straight line graph. [2]
use a graph paper instead
- (ii) Use your graph to estimate the temperature of the liquid after 35 minutes. [2]

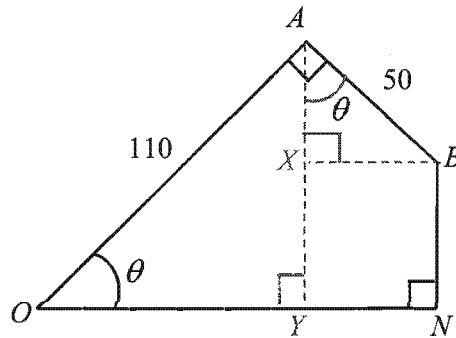
- (iii) It is given that the formula connecting T and n is $T = 28 + ae^{-kn}$, where a and k are constants.

Use your graph to estimate

- (a) the value of a and of k , [4]

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- (b) the time taken for the temperature to fall to half of its initial value. [2]



A farmer puts fences around the perimeter of his land $OABN$.

Angle $OAB = \text{angle } ONB = \frac{\pi}{2}$ and acute angle $AON = \theta$ radians.

$OA = 110$ m and $AB = 50$ m.

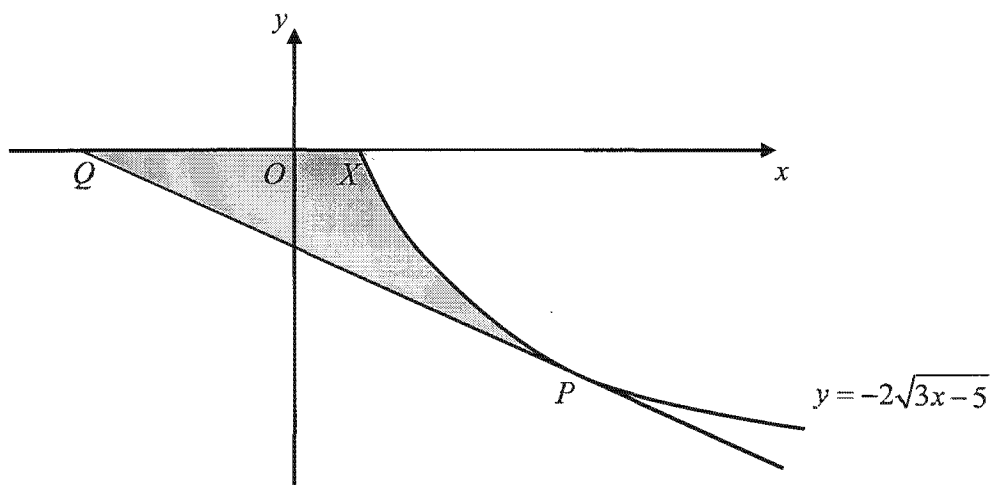
The length of fencing needed is L m.

(i) Show clearly that $L = p + 60 \cos \theta + 160 \sin \theta$, where p is a constant.

[4]

(ii) Express L in the form $p + R \cos(\theta - \alpha)$ where $R > 0$ and α is acute. [3]

(iii) Given that the farmer uses exactly 315 m of fencing, find the value of θ . [3]



- The diagram shows part of the curve $y = -2\sqrt{3x-5}$, $x \geq \frac{5}{3}$ passing through the point P where $x = 10$. The curve meets the x -axis at the point X .
- * The tangent to the curve at P meets the x -axis at the point Q .

(i) Show that the x -coordinate of Q is $-\frac{20}{3}$.

[4]

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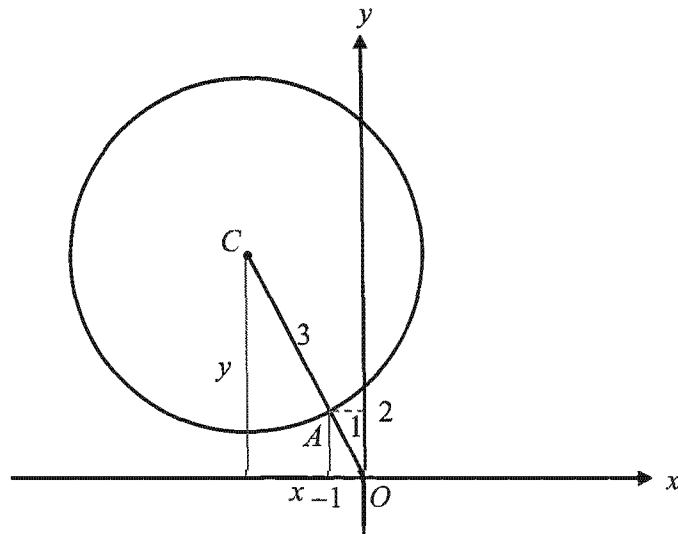
(ii) Find the area of the shaded region PQX .

[5]

- 7 (a) Show that the solution of the equation $\frac{(\log_x y)^4}{2\log_y x} + \log_3 9 = -14$ can be written in the form $y = x^k$, where k is a constant. [4]

(b) Show that $\log_5(2x-7) - \log_5(x+4) = 1$ has no real solutions.

[3]



The diagram shows a circle, centre C passing through point $A (-1, 2)$.
A line from the origin O meets C such that $CA : AO$ is $3 : 1$.

- (i) Show that the centre of the circle is $(-4, 8)$ and hence find the equation of the circle.

[3]

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- (ii) The circle is reflected along the y -axis.
State the equation of the reflected circle.

[2]

- (iii) Explain whether the point $(7, 6)$ lies on the tangent to the circle at A . [3]

- (iv) Find the equation of another tangent to the circle that has the same gradient as the tangent to the circle at A . [2]

- 9 (i) Find the value of the constant k for which $y = 2e^{-2x}x^2$ is a solution of the equation

$$4 \frac{dy}{dx} + \frac{d^2y}{dx^2} + 4y = ke^{-2x}. \quad [6]$$

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(ii) Find the exact coordinates of the stationary points of the curve $y = 2e^{-2x}x^2$.

(iii) Find the nature of the stationary points.

[3]

- 10 (i) Express $\frac{9x^2}{3x-1}$ in the form $ax+b+\frac{c}{3x-1}$, where a , b and c are constants. [1]

- (ii) Find $\int \frac{9x^2}{3x-1} dx$. [3]

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- (iii) Given that $y = 3x^2 \ln(3x-1)$, find an expression for $\frac{dy}{dx}$. [2]

(iv) Hence, evaluate $\int_1^2 x \ln(3x-1) \, dx$.

[5]

End of Paper

